

7.3 (cont.)

Review
 $\sin 75^\circ = \sin(45^\circ + 30^\circ)$

$$\sin 45 \cos 30 + \cos 45 \sin 30$$

$$\frac{\sqrt{2}}{2} \cdot \frac{\sqrt{3}}{2} + \frac{\sqrt{2}}{2} \cdot \frac{1}{2}$$

$$\frac{\sqrt{6}}{4} + \frac{\sqrt{2}}{4} = \frac{\sqrt{6} + \sqrt{2}}{4}$$

Prove: $\sec(\pi + \theta) = -\sec \theta$

$$\frac{1}{\cos(\pi + \theta)}$$

$$\frac{1}{\cos \pi \cos \theta - \sin \pi \sin \theta}$$

$$\frac{1}{-1 \cos \theta - 0 \sin \theta}$$

$$\frac{1}{-\cos \theta}$$

$$-\sec \theta = -\sec \theta \quad \checkmark$$

Ex Find $\cos(x-y)$, given $\sin x = \frac{12}{13}$, $\cos y = \frac{3}{5}$

Stay in Quad. I

$$\cos x \cos y + \sin x \sin y$$

$$\cos x \cdot \frac{3}{5} + \frac{12}{13} \sin y$$

$$\frac{5}{13} \cdot \frac{3}{5} + \frac{12}{13} \cdot \frac{4}{5}$$

$$\frac{15}{65} + \frac{48}{65}$$

$$\frac{63}{65}$$

$$\star \sin^2 x + \cos^2 x = 1$$

$$\left(\frac{12}{13}\right)^2 + \cos^2 x = 1 \quad \frac{-144}{169}$$

$$\sqrt{\cos^2 x} = \sqrt{\frac{25}{169}}$$

$$\cos x = \frac{5}{13}$$

$$\star \sin^2 y + \cos^2 y = 1$$

$$\sin^2 y + \left(\frac{3}{5}\right)^2 = 1 \quad \frac{-9}{25}$$

$$\sqrt{\sin^2 y} = \sqrt{\frac{16}{25}}$$

$$\sin y = \frac{4}{5}$$